1	Automated floorplan generation in architectural design: A review of methods and
2	applications
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# 7 1. Abstract

Accommodating predicted population growth and urbanization within the UN Climate Goals poses a significant challenge for disciplines that engage with the built environment. High performing buildings of the future should offer spatial quality for their users while utilizing resources as efficiently as possible for both construction and operation. In this review, we survey the value proposition of automatic floorplan layout generation methods and their opportunities for design guidance, feedback, and optimization in the creation of new buildings, in addition to applications for inventory characterization to survey existing housing stock and guide building policy and code. We divide existing methods into three

15 categories: *bottom-up methods, top-down methods,* and *referential methods.* We explore advantages

and challenges for each approach and propose a hybrid method for future building layout automation

17 that utilizes a new set of metrics to create sustainable buildings of the future.

18 (141 words)

19 Keywords: Floorplans, automation, generative design, buildings, sustainability, layout optimization,

20 machine learning, geometry

# 21 2. Introduction

22 The International Energy Agency (IEA) estimates that the global built floor area will increase by some

23 235 billion m<sup>2</sup> until 2050, to accommodate a growing population and rising standards of living [1]. The

- 24 environmental, economic, and ethical implications of this prediction are momentous. At a time when
- 25 humanity has around 580 Gt CO<sub>2</sub>e left to burn to keep global warming below 1.5°C, the "plan" to double
- the size of the building sector in a single generation seems risky. While one may expect significant
- 27 efficiency gains in terms of area-weighted resource use and construction costs vis-à-vis today's building
- 28 practices, the crucial question is whether humanity really needs that indoor space?
- 29 The construction sector and especially the high-performance design community have long embraced
- 30 computer-based performance analysis methods for embodied and operational energy use associated
- 31 with construction materials and building use. However, space efficiency evaluations are far less
- 32 common. Usually, there is a design brief provided to the architect that stipulates a certain amount of
- 33 program including a set percentage for circulation and space conditioning equipment. The sum of these
- 34 space uses adds up to an overall building volume that can then be explored via massing studies. The
- 35 spatial relationship between a massing volume or a floorplan and the distribution of program is, of
- 36 course, quite complex, ranging from desired adjacencies to minimal width or depth requirements. In
- 37 terms of future reuse opportunity, the design team would ideally also like to know how amenable a

- 38 given floorplan is to adaptive reuse or which walls could be load bearing while supporting good
- 39 daylighting etc.
- 40 This paper reviews previous automated floorplan layout generation methods and assesses their actual
- 41 and potential application for architectural design, urban planning, and real-estate development. A
- 42 floorplan layout creation method creates an architectural layout from a series of geometric constraints
- 43 and/or programmatic requirements. It should already be noted here that thus far only experimental
- 44 artistic architectural design practices [2,3] and the real-estate sector (Table 1) have been eager to
- 45 embrace novel generative and artificial intelligence-based layout automation tools, whereas the
- 46 architectural profession at large has expressed some reservation against algorithms whose perceived
- 47 ultimate goal might be to replace the profession. The purpose of this paper is to clarify the capabilities
- 48 and limitations of existing methods and envision how they could contribute towards the design of more
- elegant, effective, and flexible spaces on a scale ranging from individual floors and buildings to wholecities.
- 51 A number of reviews on computational layout automation have been conducted that included industrial
- 52 facility layouts [4], focused on specific computational methods, such as evolutionary algorithms [5,6] or
- agent based methods [7]. Furthermore methods have been surveyed with a focus on methods
- 54 optimizing for energy usage [8,9]. In this manuscript, we initially review which professions have thus far
- used automated space layout methods and for what purpose. We then introduce a new approach that
- 56 productively combines these methods with a specific focus on early-stage architectural massing studies
- 57 and existing building stock characterization.

## 58 3. Value proposition

- 59 The first automated floorplan generation methods were introduced close to half a century ago. The
- 60 underlying motivation has changed over time and still varies significantly between different projects and
- 61 tools today. This section provides an account of significant historic precedents followed by
- 62 contemporary use cases, in which the authors see exciting, new applications of the underlying
- 63 technologies.

### 64 Past and current approaches

- 65 Automatic space layout creation methods were introduced as artistic speculations on the future role of
- 66 computers and artificial intelligence in architecture in the 1970s. Yona Friedman proposed the *Flatwriter*
- 67 [10] to generate apartment layouts that would accommodate usage preferences of all neighbors in
- 68 cooperative housing projects. Automating the layout creation process was seen as an enabler for
- 69 participatory design. Cedric Price proposed the "Generator": A reconfigurable voxel based spatial unit
- that could be reconfigured by visitors into different layouts [11]. Both pre-computational proposals
- 71 envisioned floorplans designed by a modular kit of parts in a bottom-up process.
- 72 During the late 1970s, George Stiny started working on the analysis and reproduction of building layouts
- via so-called parametric shape grammars [12]. By understand the design and spatial qualities of existing
- 54 buildings such as Palladian villas [13] or Frank Lloyd Wright's prairie houses [14], the underlying
- 75 patterns could be deployed to recreate buildings of the same type. Similarly, Christopher Alexander
- 76 represented spatial relationships in traditional architectural floorplans via relational graphs and tree

- 57 structures [15]. These abstractions were essential first steps necessary for automating the generation of
- 78 floorplans and continue to play a foundational role in contemporary computational approaches.
- 79 Grammar based design methods have been successfully implemented into computational workflows to
- 80 procedurally compute building volumes with detailed facades. Notably Esri's City Engine [16] which
- 81 integrates the CGA++ shape grammar language [17] that enables the generation of differentiated
- 82 building envelopes for visualization purposes of urban design proposals.
- 83 As of today, automated building-level layout tools have not made much headway into mainstream
- 84 architectural practice where, their use is mainly reserved for speculative design exercises or specific
- niche applications such as office furnishing and electric lighting layouts in interior design [18] or complex
- 86 programming exercised for hospitals, airports or large scale residential and commercial developments
- 87 [19–21]. For such applications, automatically generated design options can augment or replace
- 88 conventional manual design processes by offering not a single optimal solution but a family of directions
- 89 for further design exploration [22].
- 90 In contrast to architectural design, the real estate sector has enthusiastically embraced and supported
- 91 the creation of a plethora of floorplan and building automation software and practice. Several
- 92 companies of varying size now focus on the creation of automatic layout tools to assist property
- 93 developers and decision makers. They promise to maximize the potential buildable area and perform
- 94 automatic analysis of a site, creating semi-automatic feasibility studies that can inform investment
- 95 opportunities for land acquisition and maximize rentable area. Whether geared towards the real estate
- 96 industry or conceived as in-house software tools in architecture and engineering firms, most current
- 97 approaches tackle layout automation on the scale of a single building massing. They include different
- 98 apartment (or in the case of hospitality, hotel room) mixes and simplified core placements with single or
- 99 double loaded corridors. Table 1 provides a snapshot of prominent automated space layout creation
- 100 method at the time of writing.
- **101** Table 1: Representative sample of contemporary automatic space layout creation methods in practice.

Typology	Scale	Output	Client	Use case	Company Product	Name	Citation
Residential, Commercial, Mixed use	(L) Multiple buildings	Massing, architectural program	Real estate, architects	Increase speed of design	Software	Archistar	[23]
Res, Com, Mixed	(L) Multiple buildings	Massing, floorplans	Real estate	Feasibility studies, real estate	Software	Testfit	[24]
Residential	(L) Multiple buildings	Massing, architectural Program	Architects, Real estate	N/A	Software	Matterlab	[25]
Res, Com, Mixed	(L) Multiple buildings	Massing, architectural Program	Architects, Real estate	Feasibility studies, design exploration	Software	Spacemaker	[26]
Residential	(L) Multiple buildings	Massing, architectural Program	Construction company	Modular construction	Software	KREO	[27]
Res, Com, Mixed	(L) Multiple buildings	Massing	Architects, Real estate	Sustainable design, feasibility studies	Software	Digital Blue Foam	[28]
Res, Com, Mixed	(L) Multiple buildings	Massing, architectural Program	Architects	Feasibility studies, design exploration	Software	Delve	[29]
Res	(S) Single floor	Architectural layout	Architects	Feasibility	Architecture	finch 3d	[30]
Educational	(M) Single building	Architectural layout from predefined building blocks	Community	Participatory design	Government	Seismic School App	[31]
Residential	(L) Multiple buildings	Massing, architectural Program	Community, architects, real estate	Participatory design, feasibility	Government	Prism App	[32]
Undefined	(S-L)	Building massing, lighting layout, window placement	Architects, engineers	Framework for automated design	Software	Project Refinery	[33]
Residential	(L) Multiple buildings	Massing, architectural program	Architects, government	Design exploration, community engagement	Software	Typenhaus+	[34]
Undefined	(L) Multiple buildings	Massing	In-House design tool	Design exploration	Architecture	Scout	[35]

Undefined	(L) Multiple buildings	Massing, architectural program	In-House design tool	Design exploration	Engineering	Site Solve	[36]
Res, Com, Mixed	(M) Single building	Massing, architectural program	Municipalities, real estate, architects	Design exploration, feasibility	Software	Omrt ostate	[37]
Res, Com, Mixed	(L) Multiple buildings	Massing	Homeowners, real estate	Land acquisition, real estate evaluation	Software	CityBldr	[38]
Hotel	(M) Single building	Massing, architectural program	Hospitality companies	Feasibility, early-stage planning	Software	Parafin	[39]
Res, Com, Mixed	(L) Multiple buildings	Massing, architectural program	In-house	Design exploration, feasibility	Architecture	Gensler Blox	[40]
Residential	(S) Single Apartment	Furnished architectural layout	Architects	Increase speed of design	Software	PlanFinder	[41]

#### 103 *Future applications*

104 We note that there is currently no technical implementation of automatic space layout creation

available that can fully replace a skilled human designer. More importantly, given the crucial role that

architecture can play to provide more socially equitable and environmentally responsible spaces, we do

107 not believe that the end goal of automated floor-plan generator methods should be to replace the

108 human architect. Instead, we have identified three broad use cases that go beyond efficiency

109 maximization and rather focus on improving the quality of the design process and resulting architecture.

110 These use cases are design feedback, design guidance/optimization, and inventory characterization.

111

#### 112 **3.1.** Use Case 1 - Design Feedback

Building massing decisions can have a significant and hard to predict impact on resulting interior space layouts, which in turn have cascading effects on building occupancy, structural efficiency, and even

operational energy use. Fast simulations and generative design tools can help designers develop their

116 own intuition for such relationships. In structural engineering education for architects and engineers,

real-time simulations have become a useful tool to visualize problems and help designers build a

118 geometric intuition to create more efficient structures [42,43]. Real-time visualization of the impact of

design decisions can be useful to convey information to decision makers. When combined with novel

120 interfaces, non-expert stakeholders or the local community can be engaged and learn about the design

121 process more easily [44].

122 Plugging in to existing design workflows, automatic layout generation could help to visualize how

123 changes in a building's massing relates to constraints for circulation, program, or structural

124 requirements, as illustrated in Figure 1. Showcasing how building cores must be dimensioned for a given

125 floorplate and the influence of floor-plan typologies on the energy usage of a building [45] can give

architects a more intuitive understanding in early design processes. Programmatic changes based on

127 different lighting and thermal requirements can have a direct influence on a building's energy budget:

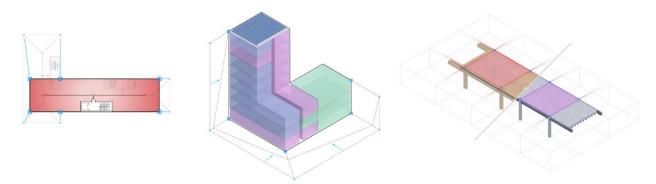
128 Interactive approaches can give a more intuitive understanding of these requirements, leading to

solutions that can negotiate between requirements of different stakeholders. Furthermore, materially

130 integrated design processes can visualize how different construction methods and material systems

131 have different constraints during the design process. A direct comparison and calculation of embodied

132 carbon and achievable spans could help users find new more sustainable design solutions [46].

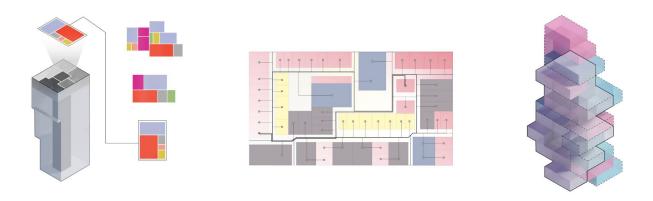


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- 134 135

Figure 1: Pedagogical use of generative design tools to help build design intuition for circulation (left), program and energy (middle) and material-based constraints (right).

#### 136 **3.2.** Use Case 2 - Design Guidance or Optimization

- 137 Generative layout tools can be used to augment different stages of existing digital design workflows.
- 138 Parametric design spaces can be explored for optimization within predefined constraints [47], and
- 139 grammar- and aggregation-based automated methods have been used to create new types of modular
- structures [48]. As speculative and early-stage design tools, automated approaches offer the
- 141 opportunity to test ideas at scale and generate design options iteratively that would be difficult to
- 142 achieve with manual workflows (Figure 2).
- 143 With highly specific programmatic requirements in specialty typologies, such as hospitals or airports,
- automated layout methods can help designers to optimize floorplans with adjacency, pathfinding,
- energetic or daylight heuristics [8,19], or structural system efficiency [49]. Multi-objective optimization
- and objective functions that are highly specific to the specified architectural problem can be used to
- 147 negotiate between different (competing or diverging) goals. A series of experimental hybrid semi-
- 148 automated methods have been deployed in such design processes where physics-based simulations can
- 149 be steered by a user to inform programmatic distribution of layouts [50].
- 150 Referential automated methods can be deployed in later stages of building design. Leveraging
- architectural catalogues and previously generated designs, methods of automation can reuse and adapt
- established design solutions for new problems. This has been successfully demonstrated on a material
- scale where algorithmic workflows can identify closest fit solutions in existing material catalogues [51]
- as well as for adaption of existing floorplan layouts into new building massing [52].
- 155

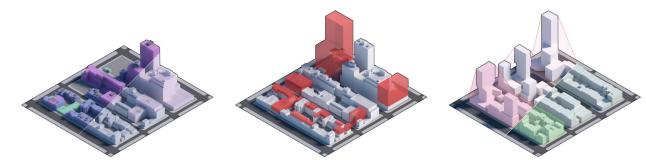


 157
 Figure 2: Use of automatic methods as design tool for automatically populating building massing (left), optimizing existing

 158
 building layouts (middle) and the creation of novel design options (right)

#### 159 **3.3.** Use Case 3 – Inventory Characterization

- 160 Automatic layout design tools not only offer opportunities for new buildings, but could be used to
- 161 characterize and redevelop existing urban environments. Making use of widely available geometric
- 162 massing GIS datasets, existing building stock could be modeled on a building level when combined with
- 163 automatic floorplan layouts. This could lead better and more detailed understanding of existing housing
- 164 stock and its embodied material quantities [46].
- 165 A better and more visual understanding of future developments enabled by current zoning could lead to
- 166 more informed decisions for housing policies and building laws and allow for non-experts from the
- 167 broader public to engage with planning processes. A clear understanding of desired goals could lead to
- 168 outcome or performance based zoning that can take metrics such as urban comfort, mobility, and
- 169 daylighting in to account [53]. Identifying possibilities of reuse or densification on a large scale could
- 170 empower lawmakers to better guide their cities development as depicted in Figure 3.
- 171



- 172
- Figure 3: Opportunities of automatic space layout tools to be utilized for the survey of existing housing stock (left), to explore
   opportunities of densification (middle) and to identify implications of changes in zoning and building codes (right).
- 175

### 176 4. Methods

- 177 Following a description of possible use cases, this section reviews the computational methods
- 178 underlying previously suggested approaches for automatic space layout generators. With origins in
- 179 various engineering and computer science disciplines, many of the methods have been developed for

- 180 different use cases and have been adapted for building design workflows. This opens the field to new
- ideas and approaches for spatial design, but can also lead to a mismatch, where methodologies have
- inherent shortcomings that are difficult to adapt to the requirements of the architecture and planning
- disciplines. We divide existing approaches into three categories: *bottom-up methods, top-down methods*
- and *referential methods*. We outline the strengths and weaknesses of these categories vis-à-vis
- 185 previously mentioned use cases.

### 186 4.1. Indexing and Search

- 187 Four main databases were used to retrieve research articles for this review paper: Web of Science [54],
- 188 Google Scholar [55], Journals indexed in the Architecture and Civil Engineering disciplines from Scopus
- 189 [56], as well as CumInCAD [57], a database of conferences and journals in the architectural
- 190 computational design disciplines. In a second step we analyzed the references mentioned in the review
- and methods articles as well as tracking novel work that cited the relevant articles. A fully automated
- search and bibliometric analysis was not possible as floorplan and layout automation keywords are used
- in different disciplines for applications in electric circuit and factory layout planning and design. We
- identified 49 different methods with geometric architectural outputs of which 14 are bottom-up, 27 are
- top-down, and 8 are referential. Methods with architectural intent that did not result in a floorplan
- 196 layout (e.g. only studied adjacency graphs in floorplans, or building massings) were excluded.

## 197 4.2. Bottom-up Methods

- 198 Architectural design briefs often have highly prescriptive spatial requirements. Because of heavily
- 199 specified room sizes or adjacency constraints, layout designs often lend themselves well to be generated
- via bottom-up design processes. Bottom-up generator methods are therefore conceptually related to
- 201 traditional design methods such as mind mapping of spatial relationships, bubble diagrams, and physical
- 202 modelmaking strategies. When using modular construction logics that make use of prefabricated
- 203 systems in concrete or timber [58] bottom-up aggregation logics enable the exploration of different
- 204 design variations and part-whole relationships.
- 205 In a final structure, a series of predefined building blocks are aggregated into a larger assembly. As
- 206 computational methods for the design of floorplans and building layouts, these aggregations can either
- 207 be static (with predetermined architectural spaces) or adaptive (changing during computation) and can
- 208 be coupled with heuristics to achieve a desired global outcome. Transformations during the aggregation
- 209 process occur on the individual parts themselves.
- 210 During the bottom-up aggregation process, additional layers of information can be superimposed on the
- digital model to either change, swap out existing units or guide further aggregations. These heuristic
- 212 methods can include analytic metrics such as spatial relationships (proximity requirements),
- 213 environmental performance (daylight access, energy usage), structural efficiency metrics, or geometric
- 214 details (proportions). A schematic of a bottom-up automatic design process for a series of rooms is
- 215 described in Figure 4. Table 2 compares different approaches and implementations of bottom-up
- 216 methods.

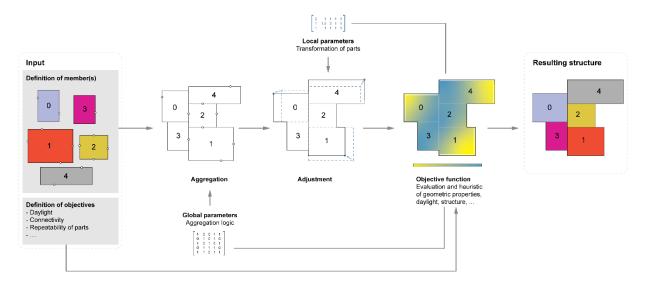


Figure 4: Schematic of bottom-up automatic space layout design methods. Starting with a definition of members and objectives, an initial aggregation and adjustment transforms the individual parts themselves. An objective function evaluates the outcome and drives local and global parameters to adjust the outcome.

221	Table 2: Comparison of bottom-up automatic space layout creation methods in literature. Genetic Algorithms (GA),
222	Mathematical programming (MP)

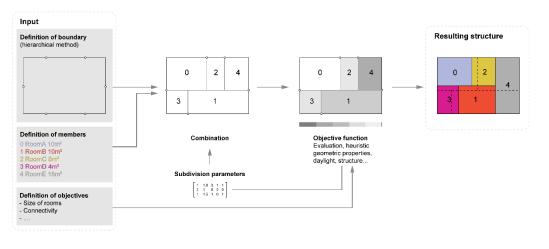
Typology	Scale	Objective Function	Optimizer	Inputs	Output	Speed	Architec tural Quality	Citation
N/A	(S) Single floor	Minimal wall length	GA	Number and areas of rooms	Floorplan, based on grid	N/A	Low	[59]
Residential	(S) Single floor	Maximize cross ventilation, (perimeter to area ratio) and minimize weighted sum of distances (closeness of rooms)	GA	Tree representation of program	Floorplan, differentiated rooms connected	N/A	Low	[60]
Public	(S) Single floor	Alignment, adjacency, orientation, proportion (of single rooms)	Physically Based	Area, adjacency	Modeling architectural design objectives in physically based space planning	N/A	Low	[61]
Residential	(S) Single floor	Minimize gap space.	Evolutionary algorithm	Area, location preference	Assigned program on existing layout, differentiated boundaries	N/A	Low	[62]
Residential	(M) Multiple floors	Connectivity, adjacency, envelope containment, convexity	1.Baysian network for Program generation, 2. Metropolis algorithm	Area, foootprint, aspect ratio, adjacency, adjacency type	Program layout	~ Seconds to 7 min	High	[63]
Residential, Office	(M) Multiple floors	Shading of neighboring building, occupied area, courtyard size	Quadratic programming, simulated annealing	Boundary, total floor area, # courtyards	Massing with specified floor area	~16 min	Medium	[64]
Office	(M) Multiple floors	Spatial configuration: semi-automatic methods for layout generation in practice	Physically Based	Area, adjacency	Program layout	N/A	Med	[50]
Residential	(M) Multiple floors	Daylight, predicted mean vote, shading	Simulated annealing	Programmatic units	Aggregation of modular programmatic units	4 min	Low	[65]
Residential	(M) Multiple floors	Maximize area in boundary, proximity and connectivity of program	Rectangular Voronoi Subdivision, Genetic Algorithm	Area, weighted adjacency matrix	Volumetric Arrangement of layout	12 min	Low	[66]
Residential	(S) Single floor	Adjacency, size	MP	600x400pixel raster image or vector graphic, area, adjacency	Layout on input image or vector graphic.	1.3-45.6 s	Medium	[67]

Residential	(S) Single floor	Connecting different room graphs to whole buildings	N/A	Programm graphs, layouts	Aggregation of multiple layouts	N/A	Medium	[68]
Residential	(M) Multiple floors	topology, room dimension and aspect ratio, building shape	Agent based	Program graph, area of rooms	Generated layout assigned to Grid voxel	~ Seconds	Low	[69]
Residential	(S) Single floor	Compactness, site boundaries, topology, user rating, circulation, privacy	GA	Areas, adjacency, window door or entrance requirement.	Program layout	6s – 7.3 h	Medium	[70]
Residential	(S) Single floor	None - Exploratory	Graph theory	Dimensional constraints, adjacency	Program layout	~ 1.5-2min	Medium	[71]

- 224 Bottom-up processes for exploratory and speculative design have been embraced by the design
- 225 community to create discrete building systems that reintegrate design thinking with computational
- 226 methods of design and means of production [72]. Applied to a building scale, they are particularly useful
- 227 when designing for specific typologies that allow for modular construction and design logics in their
- realization. Members of a structure, the so-called discrete parts, can be aggregated to respond to
- 229 specific architectural and spatial constraints or construction requirements, creating opportunities for
- robotic fabrication and reconfigurable structures [73].
- As a response to the large search spaces of bottom up design processes, the Model Synthesis algorithm
- creates a set of custom constraints that guide the aggregation of user defined modules into complex 3D
- shapes [74]. Taking the adjacencies of parts of an existing 3D shape as an input, the method can
- 234 generate new variations of larger dimensions that satisfy the original constraints. The method, also
- referred to as Wave Function Collapse (WFC), has since gained traction for creating 2D textures (using
- two dimensional pixel adjacencies) and 3D models for procedural level creation in computer games
- [75,76] as well as for modular design in the architectural domain [77]. To further guide the search
- towards solutions with controlled spatial qualities, machine learning (ML) guided heuristics have beenproposed [78].
- 240 Methods of aggregation with large geometric freedom often create large search spaces that need clever
- 241 heuristics to guide the exploration and output of good results. Additionally, stochastic methods do not
- necessarily find a solution, based on the problem settings. Furthermore, the bottom-up methods make
- it difficult to embed and control layers of hierarchy that are prevalent in architectural design such as
- 244 different levels of circulation or structural load transfer that require differentiated building components
- 245 or adjustments.

#### 246 4.3. Top-Down Methods

- 247 Real-world architectural design is often highly constrained by predefined building massing that stems 248 from urban scale considerations, building code, or regulations. This can result in highly prescriptive
- from urban scale considerations, building code, or regulations. This can result in highly prescriptive volumes that define the boundaries of a building that architects want to be fully occupied. When
- designing a building with such strong constraints on the envelope, defined through contextual
- requirements, site boundaries, or the reorganization of an existing structure, top-down design methods
- can be of interest. Methods for subdivision, fitting, shape packing, and iterative agent based methods
- have been applied across architectural scales to automate design problems (Figure 5), ranging from the
- 254 material scale with optimal placements and dimensioning of shell components [79] to the layout and
- 255 partitioning of geographical district scale [80].



256

Figure 5: Schematic of top-down automatic space layout creation methods. Starting with a definition of boundary conditions,
 members and objective functions, an initial subdivision is evaluated by the objective function. Adjustment of the subdivision
 parameters results in a final structure.

260 Two promising technological inspirations and very active areas of research originate from the VSLI

261 layout design and the Facility Layout Problem (FLP). Working with hierarchical systems that have

interconnected rectangular modules, while integrating material constraints [81], the automation of VSLI

circuits design has parallels to spatial layouts. As an optimization problem from the engineering
 community for arranging program in a given floor space, FLP is applied when machines in a factory hall

for have to be laid out for a production line [82]. There has been significant interest in trying to transfer

FLP methods to the architectural domain to optimize the placement of room layouts. However, current

267 methods for solving FLP problems make use of highly abstracted mathematical models that are difficult

to be transferred to real-world architectural environments and their implementation in available

software tools on the market has been limited [83].

270 Top-down methods take a massing or boundary as an input, as well as a series of entities as fillers or

targets for insertion. The input design is subdivided based on geometric constraints to assign spaces.

272 Compared to the bottom-up method, the transformations are done on the global boundary conditions

directly, resulting in a solution that will always conform to the initial boundary condition. An overview of

274 different top-down methods is given in Table 3.

275 Heuristics can be used to assess the current state of subdivision and can inform next steps in the case of

iterative optimization processes. This can be computed using mathematical programming, such as Mixed

277 Integer Linear Programming [84], Squarified Treemap algorithms [85] or more geometry based

278 approaches [22,86].

279 The top-down methods work best when used with fixed boundary constraints. Applied to building

design in urban environments, the massing of a building is often predetermined (or highly constrained)

281 by local building codes. In a first step, top-down approaches can be used to evaluate whether a certain

boundary condition or building massing can be filled with a desired program or functional unit. To

implement hierarchies, recursive subdivision methods that iterate over the resulting subspaces or

284 programmatic clusters. Working on the end of a hierarchical system, the top-down methods are only

able to cover a small, previously defined design space; in architectural practice that would mean that

stand alone they are less useful for exploratory design stages where the boundary conditions (e.g.

287 building massing) are not yet defined.

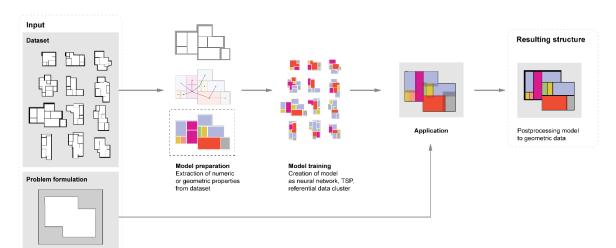
Table 3: Comparison of top-down automatic design methods in literature. Abbreviations: Genetic Algorithms (GA). Mathematical programming (MP) 289

Typology	Scale	Objective Function	Optimizer	Inputs	Output	Speed	Architectural Quality	Citation
Office	(S) Single floor	Adjacency, minimize travel distance	Quadratic assignment	Areas, adjacency	Assigned program on existing layout	High	Very Low	[87]
Office	(M) Multiple floors	Adjacency	GA	Areas, adjacency	Assigned program on existing layout	High	Very Low	[88]
Office	(M) Multiple floors	Adjacency	GA	Areas, adjacency	Assigned program on existing layout	High	Very Low	[89]
Office	(M) Multiple floors	Adjacency	GA	Areas, adjacency	Assigned program on existing layout	High	Very Low	[90]
Hospital	(M) Multiple floors	Adjacency	GA	Areas, adjacency	Assigned program on existing layout	N/A	Low	[91]
Residential	(S) Single floor	Adjacency, room size	MP	Adjacency, area, min width/depth,	Assigned program on existing layout	N/A	Medium	[92]
Residential	(S) Single floor	Adjacency, room size	GA, MP	Areas, adjacency	Design topology (with adjacencies) (tree) and assigned program on existing layout	N/A	Medium	[93]
Residential	(S) Single floor	Adjacency, heating cost, lighting cost, spatial efficiency	GA	Program description (with min and max size), bounding box	Layout in bounding box	188 s	Medium	[94]
Residential	(S) Single floor	Custom fitness	GA	Areas, adjacency, proportions, building perimeter	Assigned program on existing layout (multiples of square foot units)	600s	Low	[95]
Residential	(M) Multiple floors	Adjacency	Stochastic Search	Adjacency, perimeter	Assigned program on existing layout	N/A	Low	[96]
Residential	(M) Multiple floors	Adjacency	GA	Connectivity, area, ratio	Assigned program on existing layout	N/A	Low	[97]
Residential	(S) Single floor	Practicality, originality, user input	GA, NSGA- II	Areas	Assigned program on existing layout	N/A	Low	[98]
Residential	(S) Single floor	Aspect Ratio, area	GA	Area	Assigned program on existing layout	N/A	Low	[99]
Residential	(S) Single floor	Areas	Squarified Treemap KD Tree	Areas, connectivity	Assigned program on existing layout	N/A	High	[85]
Residential	(S) Single floor	Areas, connectivity	GA	Connectivity	Assigned program on existing layout	N/A	Low	[100]
Residential	(S) Single floor	Areas, connectivity	GA	Connectivity, hierarchy	Assigned program on existing layout	N/A	Low	[101]
Residential	(M) Multiple floors	Areas, Connectivity, Material constraints	Non-linear least squares	Connectivity, Areas, Wall fabrication specification	Rooms inside boundary, precast concrete walls	2-3.5 s Seconds	Med	[102]
Residential	(S) Single floor	Areas, connectivity	GA	Connectivity, hierarchy	Assigned program on existing layout	N/A	Low	[103]
Residential	(M) Multiple floors	Adjacency, thermal performance	MP	Areas, connectivity	Assigned program on existing layout	N/A	High	[104]
Office	(M) Multiple floors	Gap spaces	MP	Room templates	Rooms tiles in existing grid	Minutes ~80s	Med	[105]
Trade Fair	(S) Single floor	Mobility, accessibility and coziness of agent- based crowd simulation	Stochastic, Simulated annealing	Agent behavior	Rooms inside boundary	2 - 7 Minutes	High	[106]
Office	(S) Single floor	Compactness	GA	Program description, ~47 geometric properties	Room tiles in existing grid	~520s Minutes	Low	[107]
Hospitals	(S) Single floor	Fitted program, view, travel	K-D Tree, Human evaluation	Program description,	Rooms inside boundary	N/A	Med	[19]

		distance, proportion						
Trade Fair	(S) Single floor	Congestion, exposure	ga, NSGA- II	Boundary, program description	Program distributed in boundary	5 days 20s per iteration	Med	[108]
Residential, office	(S) Single floor	Gap area	MIQP	Site boundary, program description,	Rooms inside boundary	~15 s Seconds	High	[84]
Generic	(S) Single floor	Orientation, adjacency, user selected subdivision grammar	Optimizer ( N/A) + Reinforce- ment learning	Site boundary, program description	Rooms inside boundary	N/A	High	[109]
Generic	(S) Single floor	Visibility, Tree Depth, Entropy	Covariance Matrix Adaptation	Parametrized geometric model	Optimized wall layout	2.25 - 7.41 s Seconds	Med	[110]

#### 292 4.4. Referential Methods

- 293 Learning from precedent has a rich tradition in architectural education and practice. Distributing design
- culture through "peer reviewed" publications of magazines and monographs (a publication describing
- the body of work of a single architect or architecture office) or through historical or topic specific
- anthologies and catalogues has analogies to the scientific community. Standardized reference works
- 297 outlining basic architectural design strategies [111–114] are used for teaching the design of building
- 298 layouts. In both professional and educational settings, they are used as reference books for
- dimensioning of standardized building elements, such as stairwells, circulation, escalators, or bathroomlayouts.
- 301 With technological advances in computation and ML, there has been a renewed interest in referential
- 302 automatic layout methods. A high-level overview of the referential method is given in Figure 6 and a
- 303 comparison of different methods in literature in Table 4.



#### 304

Figure 6: Schematic of referential automatic space layout creation methods. Starting with a dataset (catalogue) of existing
 structures. A desired property is extracted from the dataset and a model prepared and trained as Neural Net, TSP or referential
 data cluster. The model is applied to a user specified problem formulation and postprocessed into geometric data resulting in a
 final structure.

310 Table 4: Comparison of referential automatic layout design methods

Typology	Scale	Database	Reference Source	Matching	Inputs	Output (D) Direct (P) Post Processed	Speed	Architectural Quality	Citation
Residential	(S) Single Floor	101 single story houses [115]	256 × 256 pixel image, Color Coded	pix2pix NN via RunwayML	Boundary	Rooms color coded in boundary (D), manual tracing for vectors (P)	N/A	Low	[116]
Residential	(S) Single Floor	RPLAN [117]	256 × 256 pixel image, Color Coded	1. CNN for location of program 2. CNN for placement of walls	Entrance, apartment boundary	Wall map (D), vector representation of layout (P)	4 s (Seconds) (Generation) 7 Days (ML Training)	Medium	[117]
Commercial Residential Industrial	(S) Single Floor	700 annotated plans (Boston, USA, collected by author)	? x ? px Image, color coded	pix2pix NN	Boundary of building	Rooms color coded in boundary (D), manual tracing for vectors (P)	N/A	Low	[118]
Residential	(S) Single Floor	500 floorplans, undisclosed	Program graph	Bayesian model, scored adjacency graph	Apartment type	Program graph	N/A	(No architectural representation)	[119]
Residential	(S) Single Floor	RPLAN [117]	128 x 128 pixel image, color coded	1. GNN, CNN program distribution, 2. CNN floorplan image	Entrance, Apartment Boundary, Number/Ty pe of rooms	128 × 128 floorplan image (D), vectorized floorplan (P)	0.4s (Seconds) (Generation)	Medium	[120]
Residential	(S) Single Floor	117,587 Layouts from Lifull [121]	256 x 256 pixel image, program graph	Conv-MPN	Bubble diagram, (Program graph)	Room masks (D), fitted rectangles as rooms (P)	N/A	Medium	[122]
Office	(M) Multiple Floors	120,000 volumetric designs (by authors)	Voxel graph, program graph	1. GNNs for the pro- gram graph 2. GNN voxel graph,	Program Graph, User input during generation.	Volumetric pixel grid representation of program	N/A (Generation) 20 minutes (with user interaction)	Low	[123]
Residential	(S) Single Floor	RPLAN [117]	RPlan images parsed as program graph	1. Relational GAN, 2. Conv-MPN	Program graph	Vector representation of layout	<0.4s ~Realtime (Generation)	High	[124]

312 Several algorithmic methods for referential design have been used, the most prominent are ML-

algorithms with deep neural networks such as generative adversarial networks (GANs), as well as

314 mathematical programming methods to find closest matches.

- 315 A series of databases have been ported to be used for generative or transfer purposes and converted to
- 316 annotated images or graph structures. For the creation of functional relationships between programs
- 317 [63] 120 commercial real estate plans for single family houses were encoded as graphs [125]. A
- 318 Japanese real-estate image databases from the with 5.3 Million images [121] was ported for the use
- 319 with ML algorithms [122]. To more effectively train neural networks, a series of residential floorplan
- datasets were manually collected and annotated by researchers resulting in RPLAN with 80,000
- 321 floorplans [117], Rent 3D with 215 floorplans [126] and CubiCasa5K with 5,000 floorplans from Finnish
- 322 real-estate marketing material [127]. In industry, floorplan databases enable algorithmic lookup and
- reuse of floorplan drawings from previous work in the development of new layouts [41,52].
- 324 The combination of large image libraries of floorplans with GANs enabled the creation of programmatic
- infills into arbitrary floorplan shapes for apartment layouts [116] and allowed for the transfer of
- different historical architectural styles to apartment floorplans [118]. Recognizing the importance of
- 327 hierarchies, strategies such as sequential infills (starting with the living room as high importance) [84] or
- additional graph networks that inform the generation [120] or training data [122,124] highly improve
- the plausibility of generated floorplans. Featuring online web interfaces, users can manipulate
- programmatic graphs while seeing a corresponding architectural layout in real time [120,123,124].
- However, an emphasis is laid on connectivity of rooms and their sizes or boundary conditions could not
- be influenced.
- 333 The image-based machine learning methods, however, only work on very constrained boundaries and
- 334 small scales, as all information has to be encoded in a 256x256 pixel image. Even though they can be
- very accurate inside of a specific domain and create diverse solutions, because of scale limitations, they
- have only been applied to single story residential apartment layouts so far. Furthermore, the fuzzy

- outputs of image-based ML algorithms require significant postprocessing to recreate usable geometries,
- 338 while using significant computational power and greatly varying in speed.
- 339 The strong dependence of the qualities of the outputs on good datasets, makes the lack of involvement
- of a diverse representation of the design community highly problematic. The large-scale datasets used
- 341 so far in research are based on availability and have not been peer-reviewed or curated appropriately
- 342 for architectural, spatial, or cultural qualities or environmental impact, creating unpredictable outputs.
- 343

# 344 5. Discussion

The previous sections summarize the substantial effort that has already gone into automated space layout generation with existing methods borrowing heavily from advanced computational design and

- 347 machine learning approaches. It seems obvious that the real estate sector would embrace methods that
- can provide vital statistics on the marketability of a given massing, such as the number of housing units
- that can fit or the ratio of rentable to circulation areas. Given that an automated floorplan algorithm
- 350 combined with a structural sizing tool can deliver a set of drawings that can, in principle, go through
- 351 permitting and be constructed, it seems equally intuitive that many architects eye such methods with
- 352 suspicion. The level of detail that such methods provide can create an impression of finality that one
- traditionally only encounters during later design stages. There is perceived real risk that architects
- further lose control of the design process at a time when only 2% of US homes are designed by licensed
- 355 architects. Will that number fall even lower?
- We find such thinking somewhat defensive. Rather than hanging on to the *last* 2%, should the
- 357 profession not focus on the *lost* 98% by creating the best possible design in the most efficient manner?
- How can the disciplinary knowledge inform design automation to provide better quality and more
- 359 resource efficient spaces and housing?
- 360 As generative methods can produce an infinite range of different solutions a variety of heuristics are
- 361 used to classify promising solutions or guide optimization processes. This creates an opportunity to
- include building performance as a driver for design generation, extending the purely geometric
- 363 objectives such as adjacencies, position, or aspect ratio. Validated methods for building energy
- 364 simulation and natural ventilation with EnergyPlus [128], and daylight simulation using Radiance [129]
- have been integrated into layout automation workflows [8,104,130]. Metrics further expanded to
   include views [110] and agent based simulated of human behavior for both characterization and
- 367 generation of new floorplans [106,131–133].
- 368 A big challenge in the creation of coherent layouts is the problem of scale. As programmatic
- 369 requirements get more complex it becomes more difficult to coherent layouts that can integrate layers
- of hierarchy. This requires either a multi-step approach where programmatic units are clustered
- together and subdivided individually [84] or smaller units (such as a single apartment) are created on
- their own and then assembled as units into a larger buildings [130]. Hierarchical approaches have also
- been successfully implemented to inform ML models, where placing the living room first in the creation
- of apartment floorplans increased the quality of solutions [117].

- To support the creation of new hybrid methods, it is important that spatial, environmental, and
- 376 structural considerations can work in parallel and inform one another. We propose to expand the list of
- existing metrics to create workflows that can enable floorplan layouts supporting the creation of
- 378 sustainable and high performing buildings (Table 5). These metrics can be tested at various scales from
- individual room to apartment, floor, or whole buildings for performance testing and optimization.
- **380** Table 5: A new set of holistic metrics to guide automated building layouts.

Spatial	Environmental	Structural
Modularity	Daylight	Spans
Minimal change of the floorplan necessary to create different configurations while retaining same overall layout.	Provide access to daylight throughout the building, while minimizing direct solar radiation and glare.	Building layouts that work with minimal spans to reduce amounts of structural materials needed.
Compactness	Ventilation	Continuity
Reduction of circulation to fit more in a building, while minimizing unused space.	Layouts that promote natural ventilation (cross ventilation).	Layouts that stack loadbearing walls and enable optimal placement of shear walls to enable continuous carrying of loads.
Adaptability	Energy	Material Integration
Creating layouts that enable flexibility of use by the inhabitants, creating rooms that can be used for different functions or layouts that enable different uses at the same time e.g. through shielding of noise.	Minimization of building energy use by positioning and layering of less conditioned zones such as circulation to act as buffers to the conditioned spaces.	Enable layouts that promote structural material systems with low embodied carbon and integrate fabrication constraints such as prefabricated timber modules.

- 382 In addition to combining traditional floorplan generators with the above-mentioned performance
- 383 workflows, we see three specific use cases where automated floorplan methods can enrich the current
- design process.
- 385 First, for typical urban infills, arguably the most sustainable and urgently needed building typology to
- accommodate a growing population, top-down methods provide a natural starting point since many
- 387 massing parameters have already been set through zoning and setback requirements as well as clients'
- desire to maximize buildable area. There, a hybrid approach seems very promising, combining both top-
- 389 down and bottom-up methods to negotiate between programmatic requirements and the urban
- 390 context [130,134]. Referential methods be used to augment currently prevalent metrics to evaluate
- 391 layout designs, such as daylight access, aspect ratios, or material quantities, verifying the design quality
- 392 or offer alternative spatial layouts.
- 393 In the case of greenfield developments, bottom-up methods can be useful for quick design exploration
- by creating topologically different iterations. Material and construction constraints such as bay sizes,
- desired spans or prefabricated small-scale units can be integrated into the members to ensure solutions
- are feasible. Varying in resolution, the members of a bottom-up method do not have to be defined as
- 397 single rooms but could be larger units or building parts, that can be refined or filled using top-down or
- 398 referential approaches.
- 399 A third use case relates to building stock analysis. By applying floorplan generator to whole
- 400 neighborhood massing models, existing urban analysis methods from daylighting to operational and
- 401 embodied energy can be significantly refined since a floorplan help quantify the amount of material in a
- 402 building, the likely number of occupants, and the location of internal walls that block daylight.

## 403 6. Conclusions

404 In this review, we have surveyed existing automatic floorplan layout creation methods in architectural 405 design and have introduced a categorization into three methodologies. The bottom-up method 406 proposes to work with a set of parts, such as rooms or preassembled units and to aggregate them into a 407 larger structure. As an exploratory tool, it allows for the fast generation of different design options. 408 Aggregation strategies can be further coupled with heuristics to guide the assembly. However, 409 navigating often complex constraints or boundary conditions can be very challenging in the very large 410 design space. There, top-down methods can offer an alternative, starting directly from geometric 411 constraints, such as a building or site boundaries that get subdivided into smaller units. For this, 412 different subdivision or packing strategies can be deployed. Third, referential methods are being 413 investigated to make use of existing buildings and datasets. Geometric properties of existing or premade 414 layouts can be fit or adapted to a new context. Fueled by recent advances in machine learning 415 algorithms, spatial relationships have been captured as graphs or bitmap images and encoded into 416 neural networks, enabling lookup and synthesis.

417 The further accessibility of machine learning algorithms and advancements of computational tools

418 integrated into traditional geometric modeling environments used in architectural design could help

bridge the interdisciplinary gap for architects to apply more domain specific knowledge. In our survey,

420 we can show how floorplan layout automation is a dynamic field, both in terms of industry developing

421 new tools, and business cases, as well as in academic research. We can see different disciplines engaging

422 with the topic, ranging from architectural design research, civil engineering, building physics and

423 technology, as well as computer graphics.

424 Showing the opportunities of hybrid approaches that go beyond purely spatial properties (e.g.

425 proportions, areas or connectivity) to create believable floorplans, we see potential to further evaluate

426 layouts based on environmental, and structural constraints that can serve the occupants. We propose

the hybridization of the three methods, coupled with a new set of interdisciplinary metrics and

428 performance indicators to guide future building layout automation. Working together in an iterative

loop, the strengths of the different strategies can be applied at different points in the design process.

430 We show how automating building layouts can have a wide range of value propositions. Current use

431 cases in the real estate industry can be expanded to create design tools that utilize automated floorplan

432 layouts to give feedback about program, occupancy, or embodied carbon in the early stages of design.

433 Using algorithmic and data driven solutions, they can optimize building layouts during the design

434 process or explore creative solutions for new construction. Furthermore, they could lead to developing a

better understanding of existing building stock or changes in building policy: empowering architects,

436 urban designers, law makers and the public to make more informed decisions towards creating

437 sustainable cities of the future.

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### 442 8. References

- M. Wörsdörfer, T. Gül, J. Dulac, T. Abergel, C. Delmastro, P. Janoska, K. Lane, A. Prag,
  Perspectives for the Clean Energy Transition The Critical Role of Buildings, Paris, 2019.
  www.iea.org.
- 446 [2] M.C. Rehm, Complicit: The creation of and collaboration with intelligent machines, Archit. Des.
  447 89 (2019) 94–101. https://doi.org/10.1002/ad.2417.
- M. Del Campo, S. Manninger, A. Carlson, Imaginary Plans the potential of 2D to 2D Style transfer
  in planning processes, Ubiquity Auton. Pap. Proc. 39th Annu. Conf. Assoc. Comput. Aided Des.
  Archit. ACADIA 2019. (2019) 412–418. ISBN: 9780578591797.
- 451[4]R.S. Liggett, Automated facilities layout: Past, present and future, Autom. Constr. 9 (2000) 197–452215. https://doi.org/10.1016/S0926-5805(99)00005-9.
- 453 [5] V. Calixto, G. Celani, A literature review for space planning optimization using an evolutionary
  454 algorithm approach : 1992-2014, in: Siggradi, Blucher Design Proceedings, 2015.
  455 https://doi.org/10.5151/despro-sigradi2015-110166.
- 456 [6] K. Dutta, S. Sarthak, Architectural space planning using evolutionary computing approaches: a 457 review, Artif. Intell. Rev. 36 (2011) 311. https://doi.org/10.1007/s10462-011-9217-y.
- J. Rhee, R. Krishnamurti, P. Veloso, J. Rhee, R. Krishnamurti, Multi-agent Space Planning A
  literature review (2008-2017), in: J.-H. Lee (Ed.), "Hello, Cult. 18th Int. Conf. CAAD Futur. 2019,
  Proc., Daejon, Republic of Korea, 2019. ISBN: 978-89-89453-05-5.
- 461 [8] T. Du, M. Turrin, S. Jansen, A. van den Dobbelsteen, J. Fang, Gaps and requirements for
  462 automatic generation of space layouts with optimised energy performance, Autom. Constr. 116
  463 (2020) 103132. https://doi.org/10.1016/j.autcon.2020.103132.
- 464 [9] T. Du, S. Jansen, M. Turrin, A. van den Dobbelsteen, Effects of Architectural Space Layouts on
  465 Energy Performance: A Review, Sustainability. 12 (2020) 1829.
  466 https://doi.org/10.3390/su12051829.
- 467 [10] Y. Friedman, Flatwriter: choice by computer, Prog. Arch. 03 (1971) 89–101.
- T. Riley, S. Deyong, M. De Michelis, P. Apraxine, P. Antonelli, T. di Carlo, B. Cline, The Changing of
  the Avant-Garde, The Museum of Modern Art; D.A.P./Distributed Art Publishers, New York, 2002.
  ISBN: 0870700049.
- 471 [12] G. Stiny, Introduction to shape and shape grammars, Environ. Plan. B Plan. Des. 7 (1980) 343–
  472 351. https://doi.org/10.1068/b070343.
- 473 [13] G. Stiny, W.J. Mitchell, The Palladian grammar, Environ. Plan. B Plan. Des. 5 (1978) 5–18.
   474 https://doi.org/10.1068/b050005.
- 475 [14] H. Koning, J. Eizenberg, The Language of the Prairie: Frank Lloyd Wright's Prairie Houses, Environ.
  476 Plan. B Plan. Des. 8 (1981) 295–323. https://doi.org/10.1068/b080295.
- 477[15]C. Alexander, A City is not a Tree, Parts 1 & 2, Archit. Forum. 122 (1965) 58–62, 58–61. ISBN: 978-4780500275108.
- 479 [16] Esri, ArcGIS CityEngine, (2022). https://www.esri.com/en-us/arcgis/products/arcgis-

- 480 cityengine/overview (accessed May 15, 2022).
- 481 [17] M. Schwarz, P. Müller, Advanced procedural modeling of architecture, ACM Trans. Graph. 34
  482 (2015) 1–12. https://doi.org/10.1145/2766956.
- 483 [18] A. Heuman, Innovator Spotlight: Part I "Designing Design Tools," (2020).
  484 https://www.youtube.com/watch?v=MicmKkkM\_30&t=1375s (accessed May 13, 2022).
- 485 [19] S. Das, C. Day, A. Hauck, J. Haymaker, D. Davis, Space plan generator, ACADIA 2016 Posthuman
  486 Front. Data, Des. Cogn. Mach. Proc. 36th Annu. Conf. Assoc. Comput. Aided Des. Archit. (2016)
  487 106–115. ISBN: 9780692770955.
- 488 [20] C. Derix, Mediating spatial phenomena through computational heuristics, Life Inf. Responsive Inf.
  489 Var. Archit. Proc. 30th Annu. Conf. Assoc. Comput. Aided Des. Archit. ACADIA 2010. (2010) 61–
  490 66. ISBN: 9781450734714.
- 491 [21] E. Finucane, C. Derix, P. Coates, Evolving Urban Structures using Computational Optimisation, in:
   492 Proc. 9th Gener. Art Conf., 2006. http://www.generativeart.com/on/cic/papersGA2006/37.htm.
- L. Wilson, J. Danforth, C.C. Davila, D. Harvey, How to Generate a Thousand Master Plans: A
  Framework for Computational Urban Design, in: Proc. Symp. Simul. Archit. Urban Des., Society
  for Computer Simulation International, San Diego, CA, USA, 2019: pp. 113–120.
- 496 [23] B. Coorey, Archistar, (2020). https://archistar.ai/ (accessed May 13, 2022).
- 497 [24] C. Harness, R. Griege, Test Fit, (2019). https://testfit.io/ (accessed May 13, 2022).
- 498[25]R. Gidei, M. Thorley, D. Flynn, Matterlab, (2019). https://www.matterlab.co/ (accessed May 13,4992022).
- 500 [26]H. Haukeland, C. Christensen, Spacemaker, (2016). https://www.spacemakerai.com/ (accessed501May 13, 2022).
- 502 [27] KREO, Modular, (2020). https://www.kreo.net/ (accessed May 13, 2022).
- 503[28]S.V. Patel, C. Weijenberg, Digital Blue Foam, (2022). https://www.digitalbluefoam.com/504(accessed May 13, 2022).
- 505 [29] Sidewalklabs, Delve, (2020). https://hello.delve.sidewalklabs.com/ (accessed May 13, 2022).
- 506 [30] J. Wallgren, Finch 3d, (2020). https://finch3d.com/ (accessed May 13, 2022).
- 507 [31] B. Wood, Seismic School App, (2019). https://seismic-school-app.io/ (accessed October 21, 2020).
- 508 [32] Mayor of London, Prism App, (2019). https://www.prism-app.io/ (accessed October 16, 2020).
- 509 [33] Autodesk, Project Refinery, (2020). https://www.autodesk.com/campaigns/refinery-beta
   510 (accessed October 21, 2020).
- 511 [34] M. Dennemark, M. Rudolph, B. Wannemacher, Form Follows You, (2020).
  512 https://formfollowsyou.com/typenhausplus/ (accessed May 13, 2022).
- 513 [35] Kohn Peterson Fox (KPF), Scout, (2020). https://scout.build/ (accessed October 30, 2020).
- 514 [36] Ramboll, SiteSolve, (2021). https://www.site-solve.co.uk/ (accessed May 16, 2022).

- 515[37]A. Andrejevic, J. Spiegeler, B. Worms, omrt ostate, (2021). https://www.omrt.tech/ (accessed516May 13, 2022).
- 517 [38] B. Copley, D. Cairns, citybldr, (2021). https://www.citybldr.com/ (accessed May 16, 2022).
- 518 [39] A. Hengels, B. Ahmes, Parafin, (2021). http://parafin3d.com/ (accessed May 16, 2022).
- 519 [40] A. Pacheco, Gensler launches Blox, an algorithm-powered design visualization and computation
   520 tool, Archinect.Com. (2020). https://archinect.com/news/article/150202814/gensler-launches 521 blox-an-algorithm-powered-design-visualization-and-computation-tool (accessed May 13, 2022).
- 522 [41] J. van Lith, PlanFinder, (2022). www.planfinder.xyz (accessed May 16, 2022).
- [42] R.G. Black, S. Duff, A model for teaching structures: Finite element analysis in architectural
   education, J. Archit. Educ. 48 (1994) 38–55. https://doi.org/10.1080/10464883.1994.10734621.
- 525[43]T. Van Mele, L. Lachauer, M. Rippmann, P. Block, Geometry-based understanding of structures, J.526Int. Assoc. Shell Spat. Struct. 53 (2012) 285–295. https://block.arch.ethz.ch/brg/files/2012-jiass-527vanmele-lachauer-rippmann-block\_1380094579.pdf.
- 528 [44] E. Ben-Joseph, H. Ishii, J. Underkoffler, B. Piper, L. Yeung, Urban simulation and the luminous
  529 planning table: Bridging the gap between the digital and the tangible, J. Plan. Educ. Res. 21
  530 (2001) 196–203. https://doi.org/10.1177/0739456X0102100207.
- 531 [45] T. Dogan, E. Saratsis, C. Reinhart, The optimization potential of floor-plan typologies in early
  532 design energy modeling, in: 14th Int. Conf. IBPSA Build. Simul. 2015, BS 2015, Conf. Proc., 2015:
  533 pp. 1853–1860.
- 534 https://web.mit.edu/sustainabledesignlab/publications/BS2015\_FloorPlanOptimisation.pdf.
- 535[46]R.E. Weber, C. Mueller, C. Reinhart, Generative Structural Design for Embodied Carbon536Estimation, in: Proc. IASS Annu. Symp. 2020/21 7th Int. Conf. Spat. Struct., 2021.
- 537 [47] N.C. Brown, V. Jusiega, C.T. Mueller, Implementing data-driven parametric building design with a
  538 flexible toolbox, Autom. Constr. (in press) (2020) 103252.
  539 https://doi.org/10.1016/j.autcon.2020.103252.
- 540 [48] O. Tessmann, A. Rossi, Geometry as Interface: Parametric and Combinatorial Topological
  541 Interlocking Assemblies, J. Appl. Mech. 86 (2019) 1–13. https://doi.org/10.1115/1.4044606.
- 542 [49] Y. Zhang, C. Mueller, Shear wall layout optimization for conceptual design of tall buildings, Eng.
  543 Struct. 140 (2017) 225–240. https://doi.org/10.1016/j.engstruct.2017.02.059.
- 544[50]L. Helme, C. Derix, Spatial configuration: Semi-automatic methods for layout generation in545practice, J. Sp. Syntax. 5 (2014) 35–49.
- 546 http://joss.bartlett.ucl.ac.uk/journal/index.php/joss/article/view/201/pdf.
- 547 [51] F. Amtsberg, Y. Huang, D.J.M. Marshall, K.M. Gata, C. Mueller, Structural upcycling : Matching
  548 digital and natural geometry, in: Adv. Archit. Geom., Paris, 2020.
  549 http://web.mit.edu/yijiangh/www/papers/AAG2020\_Structural\_Upcycling.pdf.
- [52] O. Green, An Introspective Approach to Apartment Design, in: DC I/O 2020, Design Computation
   Ltd., 2020. https://doi.org/10.47330/DCIO.2020.THHT2676.
- 552 [53] L. Wilson, J. Danforth, D. Harvey, N. Licalzi, Quantifying the urban experience: establishing criteria

553 554		for performance based zoning, Simul. Ser. 50 (2018) 237–244. https://doi.org/10.22360/simaud.2018.simaud.031.
55! 55(		Clarivate, Web of Science, (2022). https://clarivate.com/webofsciencegroup/solutions/web-of- science/ (accessed April 11, 2022).
55	7 [55]	Google, Google Scholar, (2022). https://scholar.google.com (accessed May 15, 2022).
558	8 [56]	Elsevier, Scopus, (2022). https://www.scopus.com/ (accessed May 15, 2022).
559 560		B. Martens, Z. Turk, T. Cerovsek, CumInCAD, (2016). http://papers.cumincad.org/ (accessed May 15, 2022).
56: 56:		G. Staib, A. Dörrhöfer, M. Rosenthal, Components and Systems, Birkhäuser, 2008. https://doi.org/10.11129/detail.9783034615662.
563 564 565 566 567	4 5 6	<ul> <li>B.M.A. Rosenman, J.S. Gero, Evolving Designs by Generating Useful Complex Gene Structures, in:</li> <li>P. Bentley (Ed.), Evol. Des. by Comput., Morgan Kaufmann, San Francisco, CA, USA, 1999: pp. 345–364.</li> <li>http://pdf.aminer.org/000/743/586/evolving_design_genes_in_space_layout_planning_problem s.pdf.</li> </ul>
568 569 570	9	M. ROSENMAN, Evolutionary Case-Based Design, in: C. Fonlupt, JK. Hao, E. Lutton, M. Schoenauer, E. Ronald (Eds.), Artif. Evol., Springer Berlin Heidelberg, Berlin, Heidelberg, 2000: pp. 53–72. https://doi.org/10.1017/S0890060400141022.
57: 57:		S.A. Arvin, D.H. House, Modeling architectural design objectives in physically based space planning, Autom. Constr. 11 (2002) 213–225. https://doi.org/10.1016/S0926-5805(00)00099-6.
573 574 575	4	M. Inoue, H. Takagi, Layout algorithm for an EC-based room layout planning support system, SMCia/08 - Proc. 2008 IEEE Conf. Soft Comput. Ind. Appl. (2008) 165–170. https://doi.org/10.1109/SMCIA.2008.5045954.
57) 57		P. Merrell, E. Schkufza, V. Koltun, Computer-Generated Residential Building Layouts, ACM Trans. Graph. 29 (2010) 1–12. https://doi.org/10.1145/1882261.1866203.
578 579		F. Bao, D.M. Yan, N.J. Mitra, P. Wonka, Generating and exploring good building layouts, ACM Trans. Graph. 32 (2013). https://doi.org/10.1145/2461912.2461977.
58) 58: 58:	1	H. Yi, Y.K. Yi, Performance based architectural design optimization: Automated 3D space layout using simulated annealing, 2014 ASHRAE/IBPSA-USA Build. Simul. Conf. (2014) 292–299. http://www.scopus.com/inward/record.url?scp=84938862924&partnerID=8YFLogxK.
583 584 585	4	I. Chatzikonstantinou, A 3-Dimensional Architectural Layout Generation Procedure for Optimization Applications : DC-RVD, Proc. 2014 ECAADe Conf. 1 (2014) 287–296. http://papers.cumincad.org/cgi-bin/works/paper/ecaade2014_163.
58) 58		H. Hua, Irregular architectural layout synthesis with graphical inputs, Autom. Constr. 72 (2016) 388–396. https://doi.org/10.1016/j.autcon.2016.09.009.
588 589		B. Dillenburger, Raumindex. Ein datenbasiertes Entwurfsinstrument, ETH Zurich, 2016. https://doi.org/https://doi.org/10.3929/ethz-b-000161426.
590	0 [69]	Z. Guo, B. Li, Evolutionary approach for spatial architecture layout design enhanced by an agent-

- 591
   based topology finding system, Front. Archit. Res. 6 (2017) 53–62.

   592
   https://doi.org/10.1016/j.foar.2016.11.003.
- A. Bahrehmand, T. Batard, R. Marques, A. Evans, J. Blat, Optimizing layout using spatial quality
   metrics and user preferences, Graph. Models. 93 (2017) 25–38.
   https://doi.org/10.1016/j.gmod.2017.08.003.
- 596 [71] S. Bisht, Transforming an Adjacency Graph into Dimensioned Floorplan, 0 (2022) 1–18.
  597 https://doi.org/10.1111/cgf.14451.
- 598 [72] J. Sanchez, Architecture for the Commons: Participatory Systems in the Age of Platforms,
   599 Routledge, 2020. ISBN: 9781138362369.
- 600 [73] G. Retsin, Toward Discrete Architecture: Automation takes Command, in: Ubiquity Auton. Pap.
  601 Proc. 39th Annu. Conf. Assoc. Comput. Aided Des. Archit. ACADIA 2019, 2019: pp. 532–541. ISBN:
  602 9780578591797.
- 603 [74] P. Merrell, D. Manocha, Model synthesis: A general procedural modeling algorithm, IEEE Trans.
  604 Vis. Comput. Graph. 17 (2011) 715–728. https://doi.org/10.1109/TVCG.2010.112.
- 605[75]A. Newgas, Tessera: A Practical System for Extended WaveFunctionCollapse, Association for606Computing Machinery, 2021. https://doi.org/10.1145/3472538.3472605.
- 607[76]M. Gumin, Wave Function Collapse, (2021). https://github.com/mxgmn/WaveFunctionCollapse608(accessed May 15, 2022).
- 609 [77] J. Tóth, J. Pernecký, MONOCEROS, (2021). https://monoceros.sub.digital/ (accessed May 16,
  610 2022).
- 611 [78] T. Hosmer, P. Tigas, D. Reeves, Z. He, Spatial assembly with self-play reinforcement learning, in:
  612 Proc. 40th Annu. Conf. Assoc. Comput. Aided Des. Archit. Distrib. Prox. ACADIA 2020, 2020: pp.
  613 382–393. ISBN: 9780578952130.
- 614 [79] T. Schwinn, A. Menges, Fabrication Agency: Landesgartenschau Exhibition Hall, Archit. Des. 85
  615 (2015) 92–99. https://doi.org/10.1002/ad.1960.
- 616 [80] D. DeFord, M. Duchin, J. Solomon, Recombination: A Family of Markov Chains for Redistricting,
   617 Harvard Data Sci. Rev. (2021). https://doi.org/10.1162/99608f92.eb30390f.
- [81] N.A. Sherwani, Algorithms for VLSI Physical Design Automation, Springer US, Boston, MA, 1993.
   https://doi.org/10.1007/978-1-4757-2219-2.
- 620 [82] P. Pérez-Gosende, J. Mula, M. Díaz-Madroñero, Facility layout planning. An extended literature
  621 review, Int. J. Prod. Res. 59 (2021) 3777–3816. https://doi.org/10.1080/00207543.2021.1897176.
- 622 [83] A. Drira, H. Pierreval, S. Hajri-Gabouj, Facility layout problems: A survey, Annu. Rev. Control. 31
  623 (2007) 255–267. https://doi.org/10.1016/j.arcontrol.2007.04.001.
- [84] W. Wu, L. Fan, L. Liu, P. Wonka, MIQP-based Layout Design for Building Interiors, Comput. Graph.
   Forum. 37 (2018) 511–521. https://doi.org/10.1111/cgf.13380.
- F. Marson, S.R. Musse, Automatic Real-Time Generation of Floor Plans Based on Squarified
  Treemaps Algorithm, Int. J. Comput. Games Technol. 2010 (2010) 624817.
  https://doi.org/10.1155/2010/624817.

- [86] D. Nagy, L. Villaggi, D. Benjamin, Generative urban design: Integrating financial and energy goals
  for automated neighborhood layout, Simul. Ser. 50 (2018) 190–197.
  https://doi.org/10.22360/simaud.2018.simaud.025.
- [87] R.S. Liggett, W.J. Mitchell, Optimal space planning in practice, Comput. Des. 13 (1981) 277–288.
   https://doi.org/10.1016/0010-4485(81)90317-1.
- [88] J.H. Jo, J.S. Gero, Space layout planning using an evolutionary approach, Artif. Intell. Eng. 12
   (1998) 149–162. https://doi.org/10.1016/S0954-1810(97)00037-X.
- [89] J.S. Gero, V.A. Kazakov, Evolving design genes in space layout planning problems, Artif. Intell. Eng.
  12 (1998) 163–176. https://doi.org/10.1016/S0954-1810(97)00022-8.
- R. Jagielski, J.S. Gero, A Genetic Programming Approach to the Space Layout Planning Problem,
  CAAD Futur. 1997. (1997) 875–884. https://doi.org/10.1007/978-94-011-5576-2\_67.
- [91] P.J. Bentley, The revolution of evolution in design: From coffee tables to hospitals, Proc. Recent
   Adv. Soft Comput. (1999). http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.56.909.
- 642 [92] B. Medjdoub, B. Yannou, Separating topology and geometry in space planning, CAD Comput.
  643 Aided Des. 32 (2000) 39–61. https://doi.org/10.1016/S0010-4485(99)00084-6.
- 644 [93] J.J. Michalek, R. Choudhary, P.Y. Papalambros, Architectural layout design optimization, Eng.
  645 Optim. 34 (2002) 461–484. https://doi.org/10.1080/03052150214016.
- 646 [94] R. Baušys, I. Pankrašovaité, Optimization of architectural layout by the improved genetic
  647 algorithm, J. Civ. Eng. Manag. 11 (2005) 13–21.
  648 https://doi.org/10.3846/13923730.2005.9636328.
- [95] H. Homayouni, A Genetic Algorithm Approach to Space Layout Planning Optimization, (2007) 137.
   http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.114.7729.
- 651 [96] K. Terzidis, AutoPLAN, Z Jt. Study J. (2007) 84–87.
  652 http://ftp.formz.com/jointstudy/JS2008/11AutoPlan.pdf.
- 653 [97] A. Doulgerakis, Genetic Programming + Unfolding Embryology in Automated Layout Planning,
   654 University College London, 2007. http://eprints.ucl.ac.uk/4981/.
- 655 [98] A. Banerjee, J.C. Quiroz, S.J. Louis, A model of creative design using collaborative interactive
  656 genetic algorithms, Des. Comput. Cogn. '08 Proc. 3rd Int. Conf. Des. Comput. Cogn. (2008) 397–
  657 416. https://doi.org/10.1007/978-1-4020-8728-8\_21.
- 658 [99] M.K. Thakur, M. Kumari, M. Das, Architectural layout planning using Genetic Algorithms, Proc. 2010 3rd IEEE Int. Conf. Comput. Sci. Inf. Technol. ICCSIT 2010. 4 (2010) 5–11.
  660 https://doi.org/10.1109/ICCSIT.2010.5565165.
- [100] K. Knecht, R. Koenig, Evolutionäre Generierung von Grundriss-Layouts mithilfe von
   Unterteilungsalgorithmen, Arbeitspapiere Inform. Der Archit. 10 (2011). https://e-pub.uni weimar.de/opus4/files/1653/InfAR\_10\_Layout\_Unterteilung\_pdfa.pdf.
- [101] R. Koenig, S. Schneider, Hierarchical structuring of layout problems in an interactive evolutionary
  layout system, AIEDAM Artif. Intell. Eng. Des. Anal. Manuf. 26 (2012) 129–142.
  https://doi.org/10.1017/S0890060412000030.

- 667 [102] H. Liu, Y.L. Yang, S. Alhalawani, N.J. Mitra, Constraint-aware interior layout exploration for pre668 cast concrete-based buildings, Vis. Comput. 29 (2013) 663–673. https://doi.org/10.1007/s00371669 013-0825-1.
- [103] R. Koenig, K. Knecht, Comparing two evolutionary algorithm based methods for layout
  generation: Dense packing versus subdivision, Artif. Intell. Eng. Des. Anal. Manuf. AIEDAM. 28
  (2014) 285–299. https://doi.org/10.1017/S0890060414000237.
- E. Rodrigues, A. Rodrigues, Á. Gomes, Automated approach for design generation and thermal
  assessment of alternative floor plans, Energy Build. 81 (2014) 170–181.
  https://doi.org/10.1016/j.enbuild.2014.06.016.
- 676 [105] C.H. Peng, Y.L. Yang, P. Wonka, Computing layouts with deformable templates, ACM Trans.
  677 Graph. 33 (2014). https://doi.org/10.1145/2601097.2601164.
- [106] T. Feng, L.-F. Yu, S. Yeung, K. Yin, K. Zhou, Crowd-driven mid-scale layout design, ACM Trans.
   Graph. 35 (2016) 1–14. https://doi.org/10.1145/2897824.2925894.
- [107] I.G. Dino, An evolutionary approach for 3D architectural space layout design exploration, Autom.
   Constr. 69 (2016) 131–150. https://doi.org/10.1016/j.autcon.2016.05.020.
- [108] L. Villaggi, D. Zhao, D. Benjamin, Beyond Heuristics: Novel Design Space Model for Generative
  Space Planning in Architecture, in: ACADIA, Discip. + Disrupt., 2017: pp. 436–445.
  http://papers.cumincad.org/cgi-bin/works/paper/acadia17\_436.
- [109] N. Saha, J. Haymaker, D. Shelden, Space Allocation Techniques (SAT), in: ACADIA 2020 Distrib.
   Prox., 2020: pp. 248–257. http://papers.cumincad.org/cgi-bin/works/paper/acadia20\_248.
- 687 [110] G. Berseth, B. Haworth, M. Usman, D. Schaumann, M. Khayatkhoei, M. Kapadia, P. Faloutsos,
  688 Interactive Architectural Design with Diverse Solution Exploration, IEEE Trans. Vis. Comput.
  689 Graph. 27 (2021) 111–124. https://doi.org/10.1109/TVCG.2019.2938961.
- 690 [111] E. Neufert, Bauentwurfslehre, Bauwelt-Verlag, 1936. ISBN: 978-3-658-34236-4.
- [112] T. Jocher, S. Loch, Raumplilot Grundlagen, kraemerverlag, 2012. ISBN: 978-3-7828-1551-2.
- 692 [113] O. Heckmann, F. Schneider, E. Zapel, Floor Plan Manual Housing, Fifth, rev, Birkhäuser, 2018.
   693 https://doi.org/10.1515/9783035611496.
- 694 [114] B. Bielefeld, Spaces in Architecture Areas, Distances, Dimensions, Birkhäuser, Basel, 2019.
   695 https://doi.org/10.1515/9783035619706.
- 696 [115] Zonda, House Plans, (2021). https://www.houseplans.com/ (accessed May 15, 2022).
- [116] N. Peters, Enabling Alternative Architectures Collaborative Frameworks for Participatory Design,
   Harvard, 2018. https://www.nathanpeters.us/enabling-alternative-architectures.
- W. Wu, X.-M. Fu, R. Tang, Y. Wang, Y.-H. Qi, L. Liu, Data-driven interior plan generation for
  residential buildings, ACM Trans. Graph. 38 (2019) 1–12.
  https://doi.org/10.1145/3355089.3356556.
- 702 [118] S. Chaillou, AI Architecture: Towards a New Approach, Harvard, 2019.
   703 https://doi.org/10.9783/9781949057027-006.
- 704 [119] J. Landes, H. Dissen, H. Fure, S. Chaillou, Architecture as a Graph A Computational Approach,

705 706 707		(2020). https://www.academia.edu/42059688/Architecture_as_a_Graph_A_Computational_Approach (accessed May 15, 2022).
708 709 710	[120]	R. Hu, Z. Huang, Y. Tang, O. van Kaick, H. Zhang, H. Huang, Graph2Plan: Learning Floorplan Generation from Layout Graphs, ACM Trans. Graph. 39 (2020) 1–14. https://doi.org/10.1145/3386569.3392391.
711	[121]	Lifull, Home Dataset, (2015). https://www.nii.ac.jp/dsc/idr/lifull (accessed November 21, 2020).
712 713 714	[122]	N. Nauata, KH. Chang, CY. Cheng, G. Mori, Y. Furukawa, House-GAN: Relational Generative Adversarial Networks for Graph-constrained House Layout Generation, (2020). https://doi.org/10.48550/arXiv.2003.06988.
715 716 717	[123]	KH. Chang, CY. Cheng, J. Luo, S. Murata, M. Nourbakhsh, Y. Tsuji, Building-GAN: Graph- Conditioned Architectural Volumetric Design Generation, (2021). http://arxiv.org/abs/2104.13316.
718 719	[124]	N. Nauata, S. Hosseini, KH. Chang, H. Chu, CY. Cheng, Y. Furukawa, House-GAN++: Generative Adversarial Layout Refinement Networks, (2021). http://arxiv.org/abs/2103.02574.
720 721	[125]	H. Wood, Essential House Plan Collection: 1500 Best Selling Home Plans, Home Planners, 2007. ISBN: 1931131708.
722 723 724	[126]	C. Liu, A.G. Schwing, K. Kundu, R. Urtasun, S. Fidler, Rent3D: Floor-plan priors for monocular layout estimation, Proc. IEEE Comput. Soc. Conf. Comput. Vis. Pattern Recognit. 07-12-June (2015) 3413–3421. https://doi.org/10.1109/CVPR.2015.7298963.
725 726 727	[127]	A. Kalervo, J. Ylioinas, M. Häikiö, A. Karhu, J. Kannala, CubiCasa5K: A Dataset and an Improved Multi-Task Model for Floorplan Image Analysis, Lect. Notes Comput. Sci. 11482 LNCS (2019) 28– 40. https://doi.org/10.1007/978-3-030-20205-7_3.
728 729	[128]	D.B. Crawley, C.O. Pedersen, L.K. Lawrie, F.C. Winkelmann, Energy plus: Energy simulation program, ASHRAE J. 42 (2000) 49–56. https://gundog.lbl.gov/dirpubs/46002.pdf.
730 731	[129]	R. Ward, G. and Shakespeare, Rendering with Radiance: The Art and Science of Lighting Visualization, 1998. ISBN: 0-9745381-0-8.
732 733 734	[130]	E. Rodrigues, M.S. Fernandes, Á. Gomes, A.R. Gaspar, J.J. Costa, Performance-based design of multi-story buildings for a sustainable urban environment: A case study, Renew. Sustain. Energy Rev. 113 (2019) 109243. https://doi.org/10.1016/j.rser.2019.109243.
735 736 737	[131]	V. Azizi, M. Usman, H. Zhou, P. Faloutsos, M. Kapadia, Graph-based generative representation learning of semantically and behaviorally augmented floorplans, Vis. Comput. (2021). https://doi.org/10.1007/s00371-021-02155-w.
738 739 740	[132]	D. Schaumann, S. Moon, M. Usman, R. Goldstein, S. Breslav, A. Khan, P. Faloutsos, M. Kapadia, JOIN: an integrated platform for joint simulation of occupant-building interactions, Archit. Sci. Rev. 63 (2020) 339–350. https://doi.org/10.1080/00038628.2019.1662767.
741 742 743	[133]	D. Nagy, L. Villaggi, J. Stoddart, D. Benjamin, The Buzz Metric: A Graph-based Method for Quantifying Productive Congestion in Generative Space Planning for Architecture, Technol. + Des. 1 (2017) 186–195. https://doi.org/10.1080/24751448.2017.1354617.

- [134] E. Rodrigues, A.R. Amaral, A.R. Gaspar, Á. Gomes, An approach to urban quarter design using
  building generative design and thermal performance optimization, Energy Procedia. 78 (2015)
  2000, 2004, https://doi.org/10.1016/j.acmrrg.2015.11.002
- 746 2899–2904. https://doi.org/10.1016/j.egypro.2015.11.662.